

Particle Physics at Cosmic Dawn - Part III

Focus on Dark Matter imprint

Laura Lopez Honorez

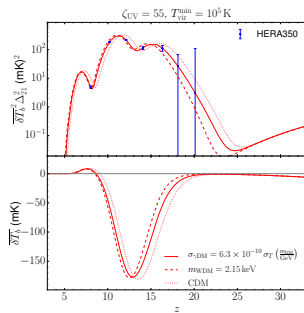
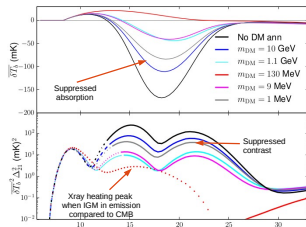


inspired by Phys.Rev.D 96 (2017) 10, JCAP 06 (2018) 007, Phys.Rev.D 99 (2019) 2, arXiv:2111.09321 in collaboration with Q. Decant, M. Escudero, J. Heisig, D. Hooper, O. Mena, S Palomares and P. Villanueva.

Frontiers of Astrophysics and Cosmology
Scuola Normale (Pisa, Italy)

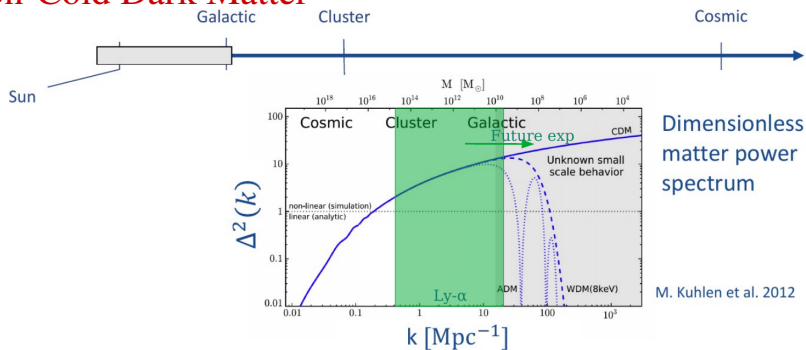
In these seminar-lectures

- Extra energy injection
 - Annihilating DM
 - Energy injection affect e.g. CMB
 - further constraints from imprint at cosmic dawn?
- Delay of structure formation
 - Non Cold Dark Matter: free-streaming, collisional damping
 - also delay in 21cm features
 - can help to disentangle NCDMs?



Non-Cold Dark Matter

Non-Cold Dark Matter

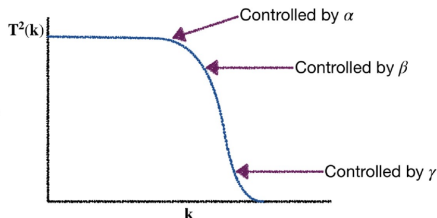


- Thermal WDM **free-streaming** from overdense to underdense regions
 \rightsquigarrow Smooth out inhomogeneities for $\lambda \lesssim \lambda_{FS} \sim \int v/adt$
- Effects $P(k)$ and $T(k)$ generalized to **Non-Cold DM** see e.g. [Bode'00, Viel'05, Murgia'17], includes NCDM **free-streaming** and **collisional damping**.

Non-Cold Dark Matter

$$T^2(k) = \frac{P(k)_{\text{nCDM}}}{P(k)_{\text{CDM}}} = [1 + (\alpha k)^\beta]^{2\gamma}$$

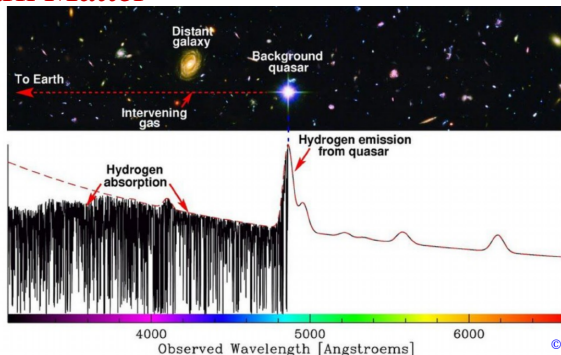
[Murgia'17]



[Courtesy DC Hooper]

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Non-Cold Dark Matter



- Thermal WDM **free-streaming** from overdense to underdense regions
 \rightsquigarrow Smooth out inhomogeneities for $\lambda \lesssim \lambda_{FS} \sim \int v/dt$
- Effects $P(k)$ and $T(k)$ generalized to **Non-Cold DM** see e.g. [Bode'00, Viel'05, Murgia'17], includes NCDM **free-streaming** and **collisional damping**.
- Thermal WDM against **Lyman- α** forest data: absorption lines along line of sights to distant quasars probe smallest structures $\rightsquigarrow m_{\text{WDM}}^{\text{thermal}} > 1.9\text{-}5.3 \text{ keV}$
 see e.g. [Viel'05, Yeche'17, Palanque-Delabrouille'19, Garzilli'19]

NCDM is not necessarily thermal Warm Dark Matter

Cosmology

$$\frac{df_{\chi}(t, p)}{dt} = \mathcal{C}[f_{\chi}]$$

Particle Physics

NCDM is not necessarily thermal Warm Dark Matter

Cosmology

$$\frac{df_{\chi}(t, p)}{dt}$$

=

$$\mathcal{C}[f_{\chi}]$$

Particle Physics

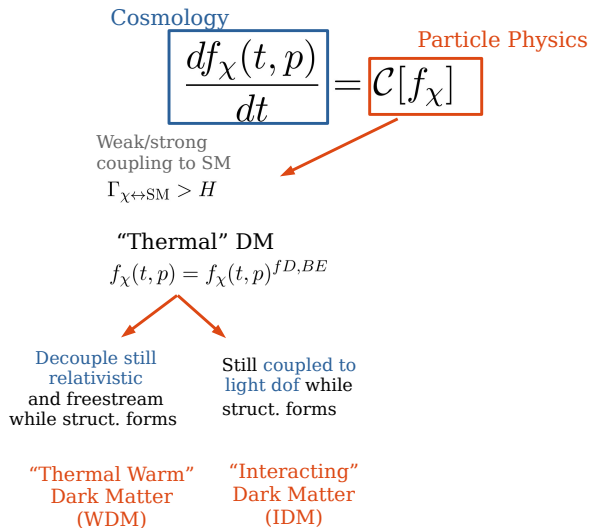
Weak/strong
coupling to SM

$$\Gamma_{\chi \leftrightarrow \text{SM}} > H$$

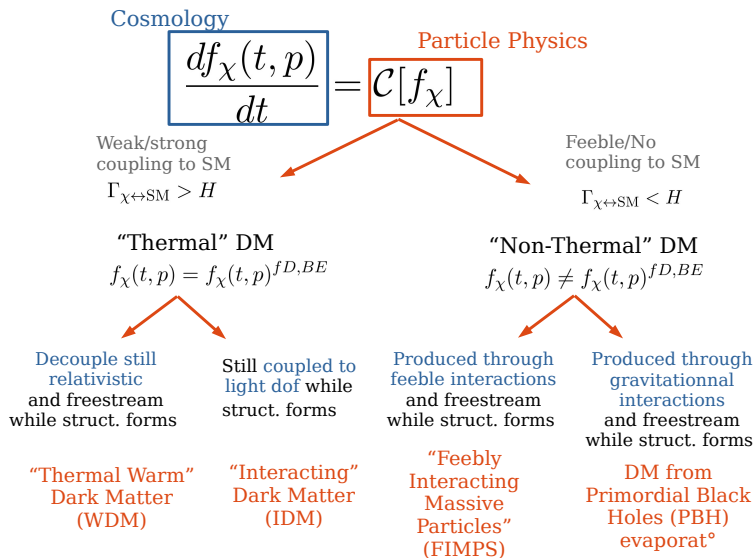
"Thermal" DM

$$f_{\chi}(t, p) = f_{\chi}(t, p)^{fD, BE}$$

NCDM is not necessarily thermal Warm Dark Matter



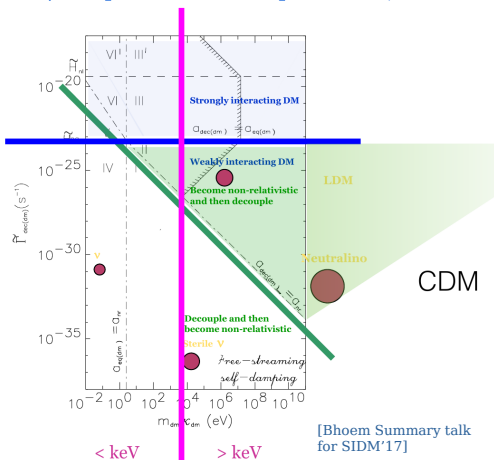
NCDM is not necessarily thermal Warm Dark Matter



NCDM is not necessarily thermal Warm Dark Matter

Classification

(astro-ph/0012504, astro-ph/0410591)



Some NCDM candidates

Thermal WDM as Free-streaming DM

NCDM as thermal WDM

Cosmology

$$\frac{df_{\chi}(t, p)}{dt} = \mathcal{C}[f_{\chi}]$$

Particle Physics

Weak coupling
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$$\Gamma_{\chi \leftrightarrow \text{SM}} > H$$

"Thermal" DM

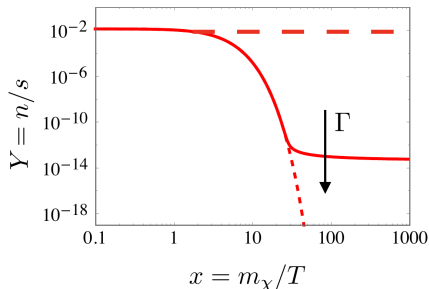
$$f_{\chi}(t, p) = f_{\chi}(t, p)^{fD, BE}$$

Decouple still
relativistic
and freestream
while struct. forms

"Thermal Warm"
Dark Matter (WDM)

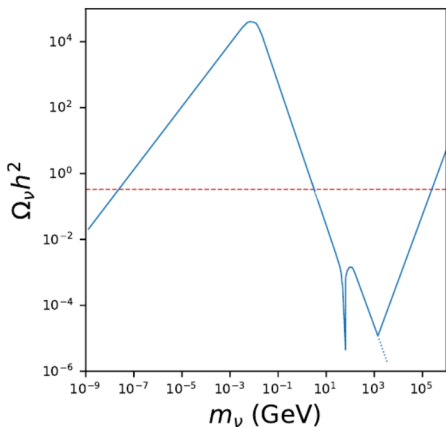
Thermal WDM freeze-out

$$\frac{df_\chi}{dt} = C_{ann}[f_\chi] \quad \rightsquigarrow \quad n_\chi \propto \frac{g_{*,S}^0}{g_{*,S}(T_D)}$$



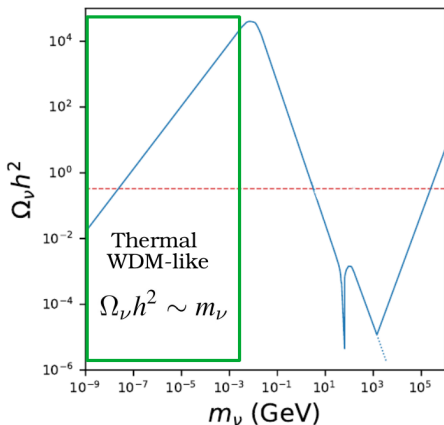
- DM annihilation driven freeze-out
- χ chem. & kin. equilibrium
- DM decouples while relativistic:
 $x_D = m_B/T_D$ and $x_D < 3$
- $\Omega_\chi h^2 = 0.12 \frac{g_\chi^{(n)} m_\chi}{6 \text{ eV}} \frac{g_{*,S}^0}{g_{*,S}(T_D)}$

Thermal WDM abundance



$$\Omega_\chi h^2 = 0.12 \frac{g_\chi^{(n)} m_\chi}{6 \text{ eV}} \frac{g_{*,S}^0}{g_{*,S}(T_D)}$$

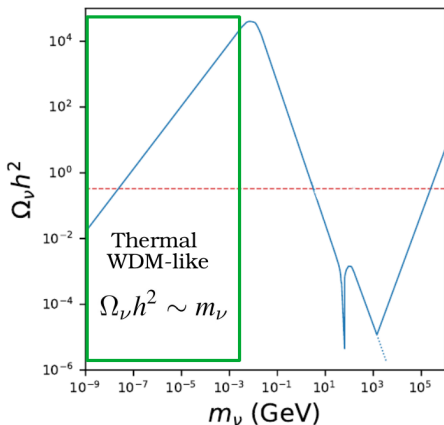
Thermal WDM abundance



$$\Omega_\chi h^2 = 0.12 \frac{g_\chi^{(n)} m_\chi}{6 \text{ eV}} \frac{g_{*,S}^0}{g_{*,S}(T_D)}$$

- **SM neutrinos** (2 dof)
 $T_D \sim \text{MeV}$, i.e. $g_{*,S}(T_D) = 10.75$
 $\rightsquigarrow \sum_\nu m_\nu \sim 10 \text{ eV}$
 for all DM (Excluded!!)

Thermal WDM abundance



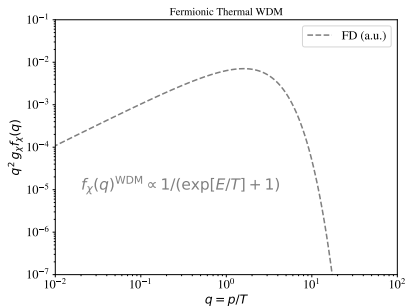
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 $\rightsquigarrow \sum_\nu m_\nu \sim 10 \text{ eV}$
 for all DM (Excluded!!)

- **Thermal WDM** (2 dof): needs $g_{*,S}(T_D) \sim 1000 \times (m_\chi/\text{keV})$ for all DM
 i.e. for few keV DM $g_{*,S}(T_D) \gg g_{SM}^{tot} \sim 100$

Thermal WDM: exponential cut in $P(k)$ at small scales

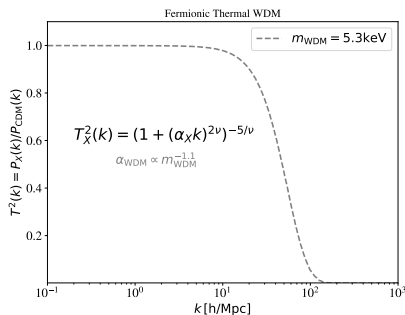
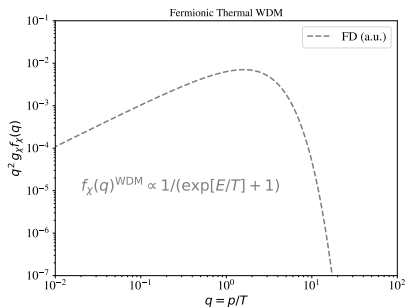
see also [Bode'00,Viel'05]



- Thermal WDM is in kinetic equilibrium thanks to fast elastic scatterings with thermal plasma: $\frac{d}{dt}f_{\chi} = C_{el}[f_{\chi}] \rightsquigarrow f_{\chi} \propto f_{\chi}^{eq}(q)$

Thermal WDM: exponential cut in $P(k)$ at small scales

see also [Bode'00,Viel'05]



- Thermal WDM is in kinetic equilibrium thanks to fast elastic scatterings with thermal plasma: $\frac{d}{dt} f_{\chi} = C_{el}[f_{\chi}] \rightsquigarrow f_{\chi} \propto f_{\chi}^{eq}(q)$
- Evolve f_{χ} up to 1st order pert. (w/ Boltzmann code as e.g. CLASS):
Transfer function $T(k) = (1 + (\alpha_{WDM} k)^{2\nu})^{-5/\nu}$ with $\nu = 1.12$ [Viel'05]

Free-streaming scale: $\alpha_{WDM} \sim 0.045 \left(\frac{m_{WDM}}{\text{keV}}\right)^{-1.11} \text{ Mpc}/h$

FIMPs as Free-streaming DM

NCDM as a FIMP

Cosmology

$$\frac{df_{\chi}(t, p)}{dt}$$

=

$$\mathcal{C}[f_{\chi}]$$

Particle Physics

Feeble/No
coupling to SM

$$\Gamma_{\chi \leftrightarrow \text{SM}} < H$$

“Non-Thermal” DM
 $f_{\chi}(t, p) \neq f_{\chi}(t, p)^{f^{D, BE}}$

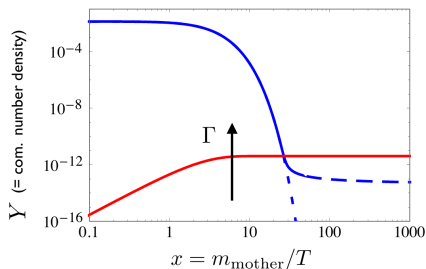
Produced through
feeble interactions
and freestream
while struct. forms

“Feebly
Interacting
Massive
Particles”
(FIMPS)

Non-thermal FIMP from Freeze-in

see also [McDonald '02; Covi'02; Choi'05; Asaka'06; Frère'06; Petraki'08; Hall'09; etc]

$$\frac{df_\chi}{dt} = C_{B \rightarrow \chi} [f_\chi] \quad \rightsquigarrow \quad n_\chi \propto \Gamma_{B \rightarrow \chi}$$



- Freeze-in from B decays
- χ decoupled
- B in chem. & kin. equilibrium
- $\Omega_\chi h^2 \propto \Gamma_{B \rightarrow \chi} M_p / m_B^2 \sim R_\Gamma$
- $\Omega_\chi h^2 = 0.12 \rightsquigarrow \lambda_\chi \lesssim 10^{-8}$
- $x = m_B/T$ and $x_{\text{FI}} \sim 3$

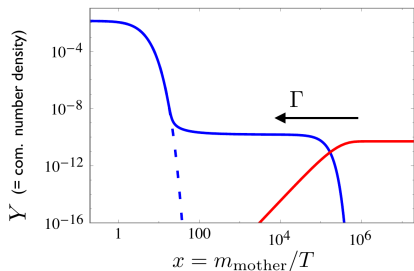
Careful: late decay (SW), production via scattering, early matter dominated era (T_R small), non renormalisable operators and thermal corrections for ultra-relativistic DM not taken into account.

Zero χ initial abundance assumed.

Non-thermal FIMP from superWIMP

see also [Covi '99 ;Feng '03]

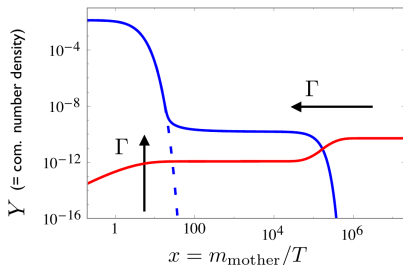
$$\frac{df_\chi}{dt} = C_{B \rightarrow \chi} [f_\chi] \quad \rightsquigarrow \quad n_\chi \propto n_B^{\text{FO}}$$



- superWIMP from late B decays
- χ decoupled
- B chem. decoupled
- $\Omega_\chi h^2 = m_\chi/m_B \times \Omega_B h^2|_{\text{FO}}$
if $B \rightarrow A_{\text{SM}} A'_{\text{SM}}$ not open
- $x = m_B/T$ and $x_{\text{SW}} \sim R_\Gamma^{-1/2} > 3$

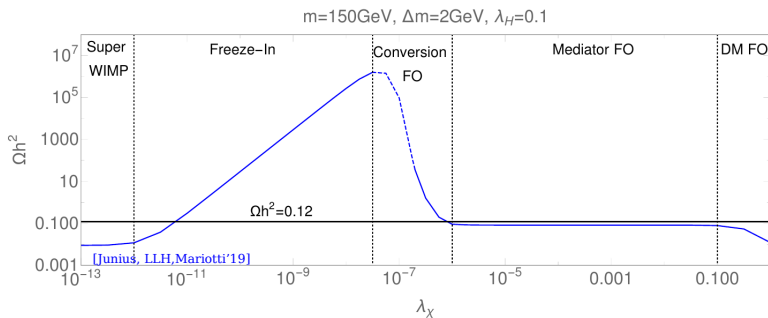
FIMPs from FI & superWIMP

Careful: both SW and FI contributions are always present for production via B decays!!

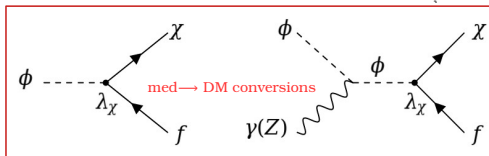
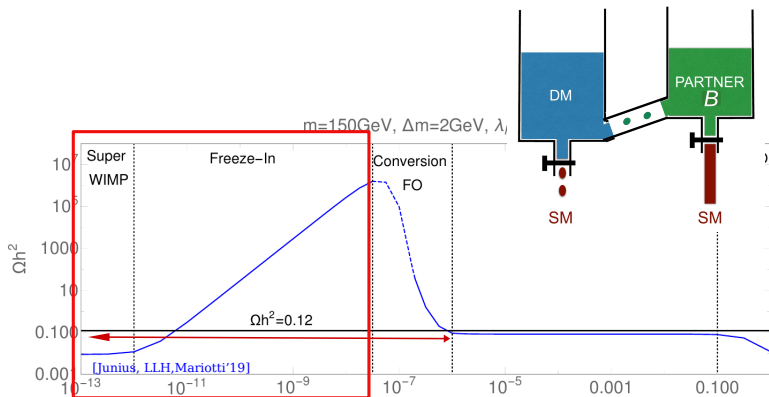


- χ decoupled
- χ population slowly builds up from B before and after FO.
- $\Omega_\chi h^2 = \Omega_\chi h^2|_{\text{FI}} + \Omega_\chi h^2|_{\text{SW}}$

Non thermal FIMP from FI and SW

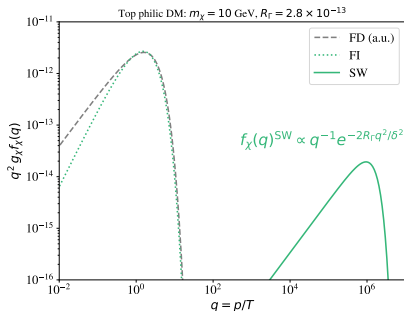
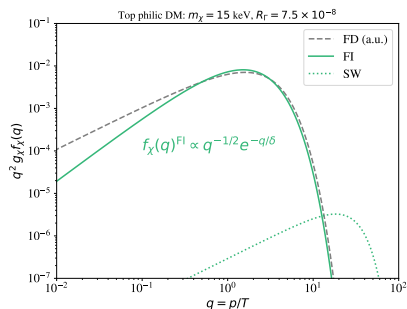


Non thermal FIMP from FI and SW



Pure FI & SW: WDM-like

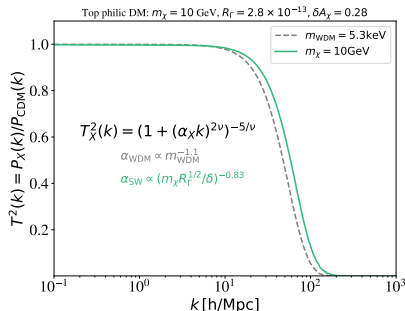
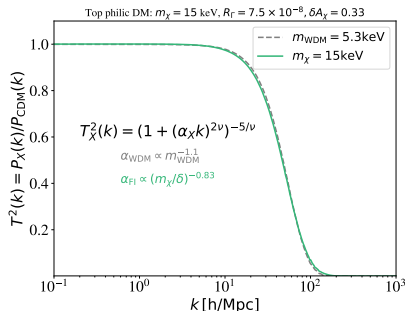
see also [Heeck'17, Boulebane'17, Kamada'19, Baumholzer'19, Ballesteros'20, d'Eramo'20]



- Contrarily to “usual” WDM, FIMPs are non-thermally produced.
Distribution $f_\chi \propto q_\star^{-\alpha} \exp(-q_\star^\beta)$ with $\alpha = \frac{1}{2}, 1$ and $\beta = 1, 2$ for FI, SW.

Pure FI & SW: WDM-like

see also [Heeck'17, Boulebane'17, Kamada'19, Baumholzer'19, Ballesteros'20, d'Eramo'20]



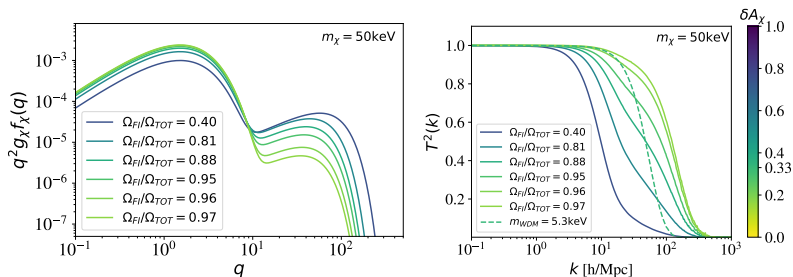
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- Using CLASS: Pure FI/SW transfer functions similar to thermal WDM.
 \rightsquigarrow Free-streaming scales [Decant, Heisig, Hooper, LLH'21]

$$\alpha_\chi \sim \begin{cases} 0.064 \times (m_\chi/\text{keV})^{-0.833} \text{ Mpc}/h & \text{for FI,} \\ 0.021 \times (m_\chi/\text{keV} \times (R_\Gamma)^{-1/2})^{-0.833} \text{ Mpc}/h & \text{for SW,} \end{cases}$$

Free-streaming scale vs Particle DM properties

- A measurement of the free-streaming scale could give an information on the DM fundamental properties (as its mass) iff we know its **production mechanism in the early universe** \rightsquigarrow need complementary DM signatures/observations to conclude.
- There exist plethora of other (mixed) free-streaming DM scenarios which $T(k)$ features will differ from Thermal WDM. For example:

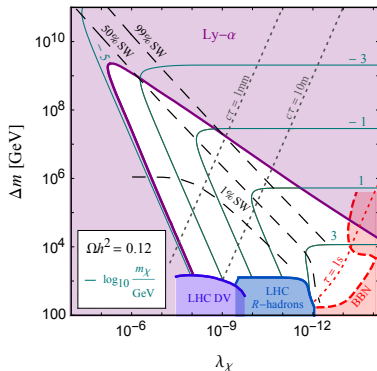
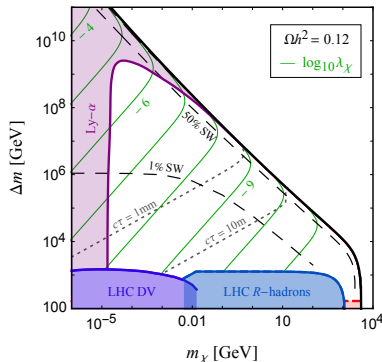
Mixed FI-SM $q^2 f_\chi$ is **multimodal** $\rightsquigarrow T^2(k) = P_{\text{FIMP}}(k)/P_{\text{CDM}}(k)$ can **significantly deviate** from e.g. WDM, α, β, γ param. or CDM+WDM



Cosmo-Particles complementarity

see also e.g. [Hall'09; Co'15; Hessler'16; d'Eramo'17; Buchmueller'17; Brooijmans'18; Belanger'18; No'19; Garmy'18; Calibbi'18,21; etc]

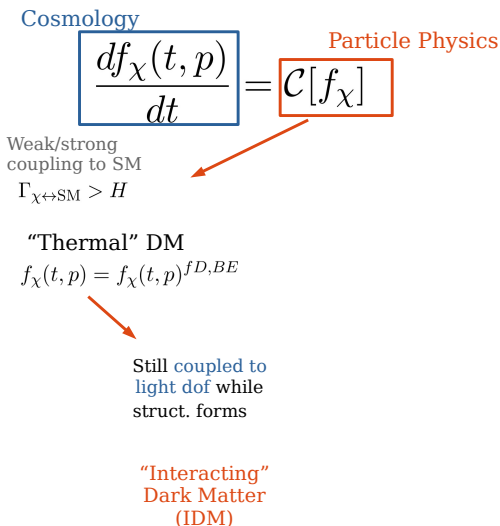
$$\text{Topphilic FIMP : } \mathcal{L} \subset \mathcal{L}_K - \frac{m_\chi}{2} \bar{\chi}\chi - m_\phi \phi^\dagger \phi - \lambda_\chi \phi \bar{\chi} t_R + h.c.$$



- Topphilic DM: Parameter space **cornered by particle** (DV + R-hadron searches at LHC - for top-philic) and **cosmology** (Lyman- α , BBN) probes.
- **Lyman- α forest data** probe DM over a large range of λ_χ , complementary to BBN for $m_\chi \sim$ few 100 GeV. **What about 21cm?**

Collisional damping
induced by DM scatterings off light dof
“Interacting DM (IDM) scenarios”

NCDM interacting with light degrees of freedom



IDM linear regime: suppressed power at small scale

Considers CDM weakly interacting with γ , ν [Bhoem'01++,Schewtschenko'14++, Olivares-Del Campo'17, etc]

- f_χ for IDM evolved to 1st order:

without DM interactions

$$\begin{aligned}\dot{\theta}_b &= k^2\psi - \mathcal{H}\theta_b + c_s^2 k^2 \delta_b - R^{-1} \dot{\kappa}(\theta_b - \theta_\gamma) \\ \dot{\theta}_\gamma &= k^2\psi + k^2 \left(\frac{1}{4} \delta_\gamma - \sigma_\gamma \right) - \dot{\kappa}(\theta_\gamma - \theta_b), \\ \dot{\theta}_{DM} &= k^2\psi - \mathcal{H}\theta_{DM},\end{aligned}$$

with DM interactions

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$$S = 3/4 \rho_\chi / \rho_\gamma, \dot{\mu} = a \rho_\chi \sigma_{IDM} / m_\chi$$

[Schewtschenko'14

IDM linear regime: suppressed power at small scale

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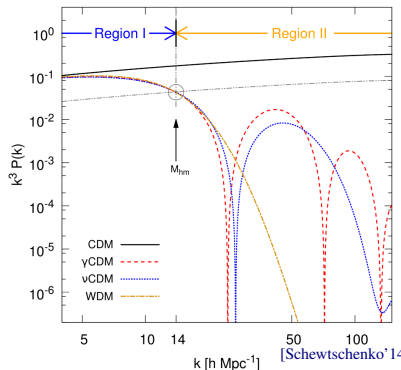
$$S = 3/4 \rho_\chi / \rho_\gamma, \dot{\mu} = a \rho_\chi \sigma_{IDM} / m_\chi$$

- Collisional damping scale

$$T_X(k) = (1 + (\alpha_X k)^{2\nu})^{-5/\nu} \quad \nu = 1.2$$

$$\alpha_{IDM} \propto (\sigma_{IDM} / m_{DM})^{0.48} \quad \text{[Bhoem'01]}$$

for IDM with γ induced damping



NCDM is not necessarily free-streaming see also [Bhoem'04,Murgia'17-18]

From linear $P(k)$ to halo mass function

NCDM non linear regime: less low mass haloes than CDM

Default extended Press-Schechter (PS) [PS'74, Bond'91] approach:

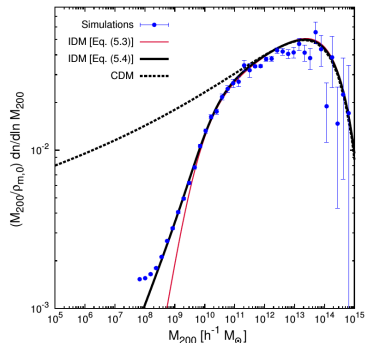
$$\frac{dn(M, z)}{dM} = \frac{\rho_{m,0}}{M^2} \frac{d \ln \sigma^{-1}}{d \ln M} f(\sigma)$$

fails to capture the suppression at low halo masses for NCDM. Some solutions in the literature:

- Consider top-hat (TH) for $W(kR)$ but correct by an extra NCDM dependent factor [Schneider'12,

Bhoem'14, Moline'16]

$$\left. \frac{dn(M, z)}{dM} \right|_{\text{NCDM}} = F_{\text{NCDM}}(M_{hm}) \times \left. \frac{dn(M, z)}{dM} \right|_{\text{NCDM, TH}}$$



IDM/WDM using $F_{\text{NCDM}}(M_{hm})$ [Moline'16]

NCDM non linear regime: less low mass haloes than CDM

Default extended **Press-Schechter (PS)** [PS'74, Bond'91] approach:

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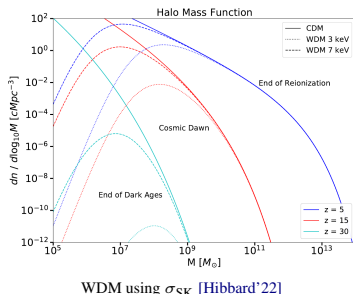
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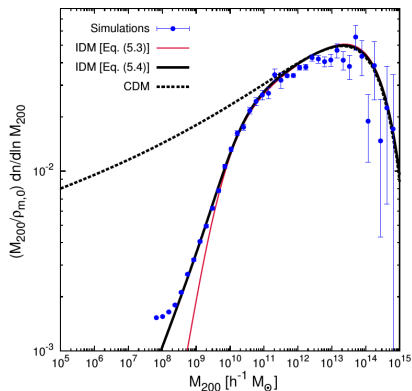
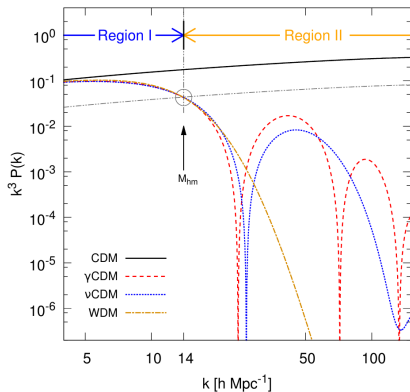
$$\left. \frac{dn(M, z)}{dM} \right|_{\text{NCDM}} = F_{\text{NCDM}}(M_{hm}) \times \left. \frac{dn(M, z)}{dM} \right|_{\text{NCDM,TH}}$$

- Consider sharp-k (SK) cutoff for $W(kR)$ in $\sigma^2 = \sigma^2(P_{lin}(k), W(kR))$ [Schneider'13, Benson'13]

$$\left. \frac{dn(M, z)}{dM} \right|_{\text{NCDM}} = \left. \frac{dn(M, z)}{dM} \right|_{\text{NCDM,SK}}$$



NB: IDM vs WDM: more low mass haloes in IDM

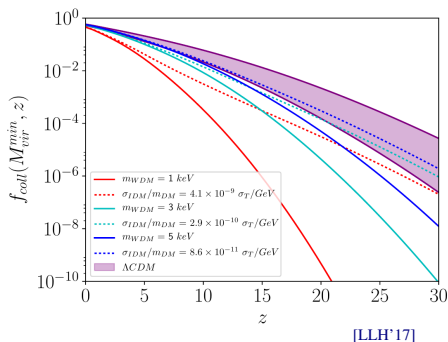


more low mass haloes in IDM than WDM at fixed α_X
 due to extra power at small scales see also ETHOS IDMs [VogelsBerger'15, Muñoz'20]

Imprint of NCDM on 21cm signal

Suppressed NCDM $f_{coll}(M_{vir})$

Remember that Ionization, heating and excitation critically depend on the fraction of mass collapsed in halos: $f_{coll}(> M_{vir}) = \int_{M_{vir}} \frac{M}{\rho_0} \frac{dn(M,z)}{dM} dM$

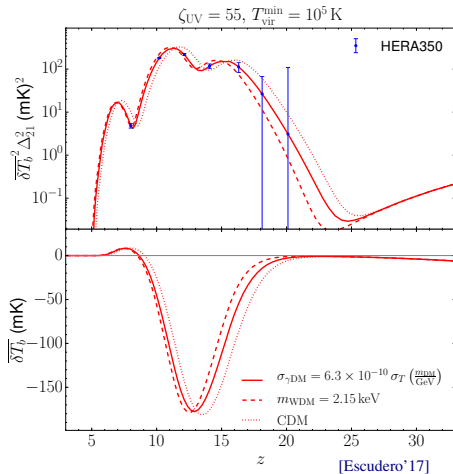


↪ more severe suppression of f_{coll} at fixed z and fixed α_X in IDM than WDM.

Delayed 21cm features for Non-CDM

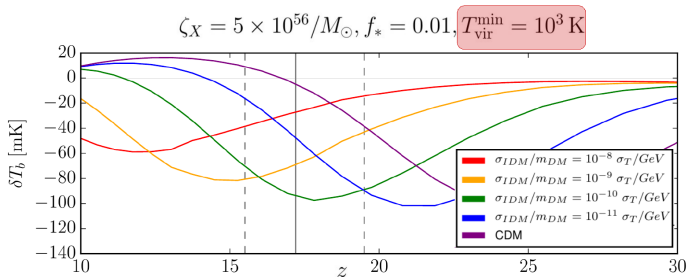
see also [Sitwell'13, Escudero'18, Schneider'18, Safarzadeh'18, Lidz'18, LLH'18, Muñoz'20, Schneider'22, Giri'22, etc]

Halo suppression can lead to **delayed astro processes** giving rise to **reionization or 21cm features**. Stronger delay for WDM than IDM.



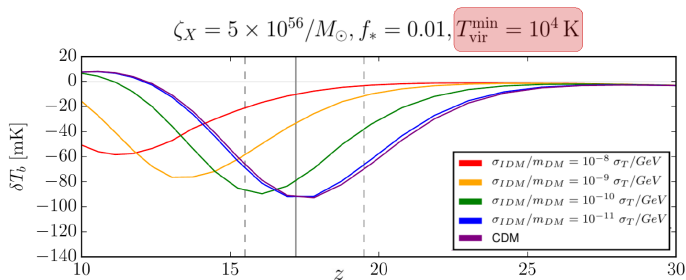
Degeneracies between NCDM effects and astro

NCDM effect degenerate with T_{vir}^{min} , f_* and L_X [LLH'18]



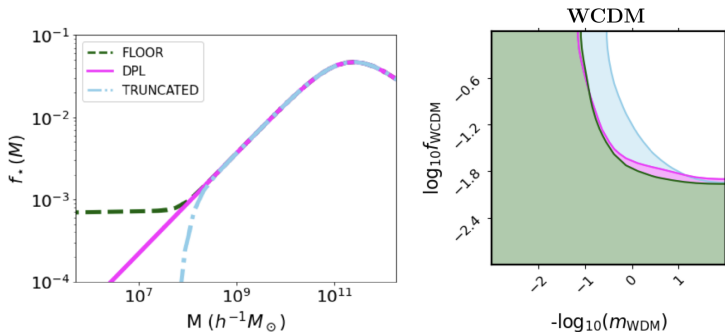
Degeneracies between NCDM effects and astro

NCDM effect degenerate with T_{vir}^{min} , f_* and L_X [LLH'18]



Forecast SKA constraints on WDM+CDM

[Giri'22] (MCMC analysis): For low minimum virial mass ($T_{vir}^{min} < 10^4 \text{K}$) and in the case that minihaloes are populated with stars, **stringent constraints** can be obtained on e.g. 100% WDM: up to $m_{\text{WDM}} < 15 \text{keV}$.

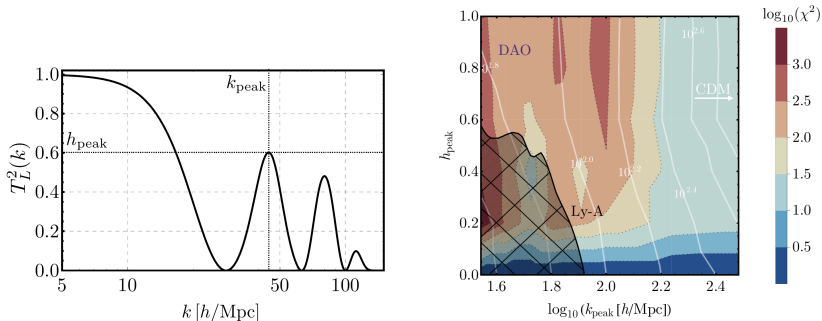


For $T_{vir}^{min} \sim 10^4 \text{K}$ it will be difficult to distinguish between an inefficient source models and a universe filled with NCDM.

Forecast HERA constraints on IDM

[Muñoz'20] (χ^2 analysis): Even considering atomic cooling ($T_{vir}^{min} = 10^4\text{K}$), HERA shall be able to :

- distinguish CDM from models with $k_{peak} < 10^{2.3}h/\text{Mpc}$
- distinguish IDMs with $h_{peak} > 0.4$ from WDM ($h_{peak} \rightarrow 0$)



More enthusiastic conclusions than [Giri'22](#)?

Conclusion

Non CDM can either be free-streaming and/or experiencing collisional damping and give rise to suppressed structure formation at small scales.

- NCDM is not necessarily thermal WDM
- Multiple DM production mechanisms can give rise to the same/similar features in Cosmology observations. Complementary observations are necessary to pinpoint the DM nature.
- Overall NCDM is expected to delay 21cm features in global signal and power spectrum.
- Future telescopes such as HERA or SKA might put stringent constraints on NCDM and distinguish between NCDM scenarios (but this might depend on T_{vir}^{min} [Giri'22])

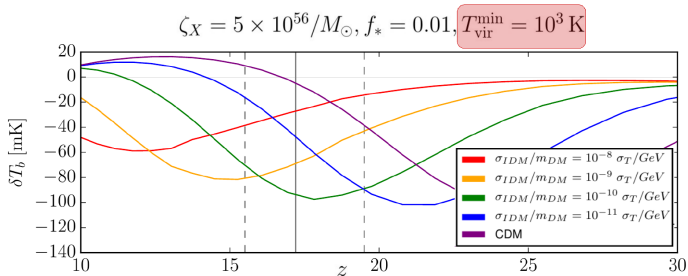
Thank you for the invitation
and for your attention!!

Backup

Imprint of NCDM on background 21cm signal

Halo suppression leads to **delayed astro processes** giving rise to 21cm features. Can be constrained by imposing **early enough absorption** [Schneider'18]

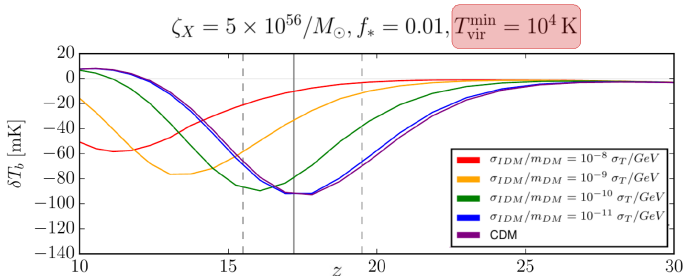
$$z(\delta T_b^{\min}) > 17.2$$



Imprint of NCDM on background 21cm signal

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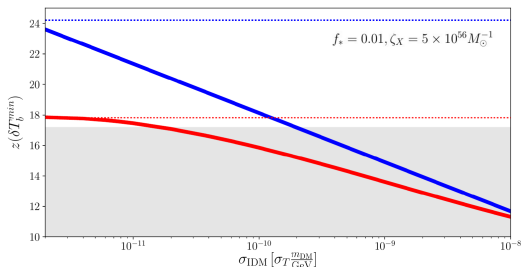
$$z(\delta T_b^{\min}) > 17.2$$



Beware important degeneracies with astrophysics ($T_{\text{vir}}^{\min}, f_*$ and ζ_X)

Constraints on NCDM from EDGES ?

- If the EDGES signal is confirmed for a fixed astro setup 21 cm can provide stringent constraints on NCDM [see also Safarzadeh'18, Lidz'18, Schneider'18]

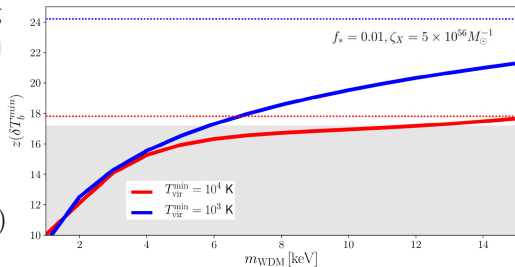


- To be compared with existing limits from Ly α forest [Yeche 17]

$$m_{WDM} > 5.3 \text{ keV}$$

and Satellite number count:

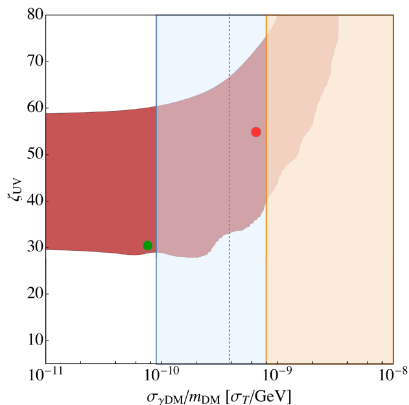
$$\sigma_{IDM} < 8 \times 10^{-10} (m_{DM}/\text{GeV})$$



BEWARE: can easily be relaxed for larger f_* !

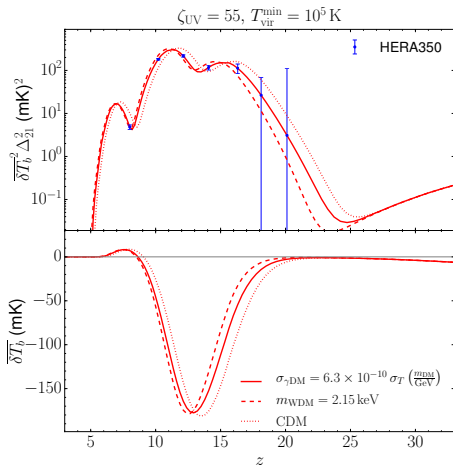
21cm could help to discriminate between Non-CDM

Halo suppression can lead to **delayed astro processes** giving rise to **reionization or 21cm features**. Stronger delay for IDM than WDM.



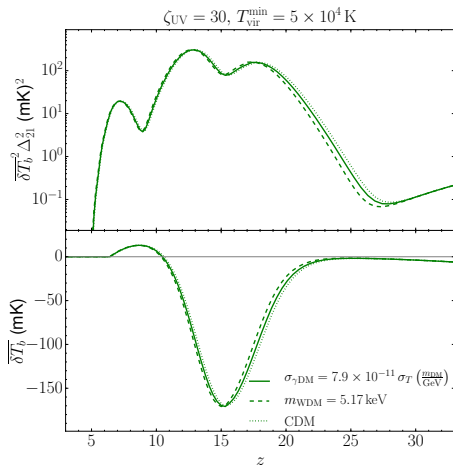
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21cm could help to discriminate between Non-CDM

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Particle physics models for DM- ν interactions

[Olivares-Del Campo '17]

Scenario	Lagrangian (\mathcal{L}_{int})	σV_t	σ_{el}
Complex DM Dirac Mediator	$-g \chi \overline{N}_R \nu_L + \text{h.c.}$	$\frac{g^4}{12\pi} \frac{m_{\text{DM}}^2}{(m_{\text{DM}}^2 + m_h^2)^2} v_{\text{CM}}^2$	$\frac{g^4}{32\pi} \frac{m_{\text{DM}}^2 y^2}{(m_h^2 - m_{\text{DM}}^2)^2}$
Real DM Dirac Mediator		$\frac{4g^4}{15\pi} \frac{m_{\text{DM}}^2}{(m_{\text{DM}}^2 + m_h^2)^2} v_{\text{CM}}^2$	$\frac{g^4}{8\pi} \frac{m_{\text{DM}}^2 y^4}{(m_h^2 - m_{\text{DM}}^2)^4}$
Complex DM Majorana Mediator		$\frac{g^4}{16\pi} \frac{m_{\text{DM}}^2}{(m_{\text{DM}}^2 + m_h^2)^2}$	$\frac{g^4}{32\pi} \frac{m_{\text{DM}}^2 y^2}{(m_h^2 - m_{\text{DM}}^2)^2}$
Real DM Majorana Mediator		$\frac{g^4}{4\pi} \frac{m_{\text{DM}}^2}{(m_{\text{DM}}^2 + m_h^2)^2}$	$\frac{g^4}{8\pi} \frac{m_{\text{DM}}^2 y^4}{(m_h^2 - m_{\text{DM}}^2)^4}$
Dirac DM Scalar Mediator	$-g \overline{\chi}_R \nu_L \phi + \text{h.c.}$	$\frac{g^4}{32\pi} \frac{m_{\text{DM}}^2}{(m_{\text{DM}}^2 + m_\phi^2)^2}$	$\frac{g^4}{32\pi} \frac{m_{\text{DM}}^2 y^2}{(m_{\text{DM}}^2 - m_\phi^2)^2}$
Majorana DM Scalar Mediator		$\frac{g^4}{12\pi} \frac{m_{\text{DM}}^2}{(m_{\text{DM}}^2 + m_\phi^2)^2} v_{\text{CM}}^2$	$\frac{g^4}{16\pi} \frac{m_{\text{DM}}^2 y^2}{(m_{\text{DM}}^2 - m_\phi^2)^2}$
Vector DM Dirac Mediator	$-g \overline{N}_L \gamma^\mu \chi_\mu \nu_L + \text{h.c.}$	$\frac{2g^4}{9\pi} \frac{m_{\text{DM}}^2}{(m_{\text{DM}}^2 + m_h^2)^2}$	$\frac{g^4}{4\pi} \frac{m_{\text{DM}}^2 y^2}{(m_{\text{DM}}^2 - m_h^2)^2}$
Vector DM Majorana Mediator		$\frac{g^4}{6\pi} \frac{m_{\text{DM}}^2}{(m_{\text{DM}}^2 + m_h^2)^2}$	
Complex DM Vector mediator	$-g_\chi Z^\mu ((\partial_\mu \chi)^\dagger \chi - (\partial_\mu \chi)^\dagger \chi) - g_\nu \overline{N}_L \gamma^\mu Z'_\mu \nu_L$	$\frac{g_\chi^2 g_\nu^2}{3\pi} \frac{m_{\text{DM}}^2}{(4m_{\text{DM}}^2 - m_{Z'}^2)^2} v_{\text{CM}}^2$	$\frac{g_\nu^2 g_\nu^2 m_{\text{DM}}^2 y^2}{8\pi m_{Z'}^2}$
Dirac DM Vector Mediator	$-g_{\chi L} \overline{\chi}_L \gamma^\mu Z'_\mu \chi_L - g_{\chi R} \overline{\chi}_R \gamma^\mu Z'_\mu \chi_R - g_\nu \overline{N}_L \gamma^\mu Z'_\mu \nu_L$	$\frac{g_\chi^2 g_\nu^2}{2\pi} \frac{m_{\text{DM}}^2}{(4m_{\text{DM}}^2 - m_{Z'}^2)^2}$	$\frac{g_\nu^2 g_\nu^2 m_{\text{DM}}^2 y^2}{8\pi m_{Z'}^2}$
Majorana DM Vector Mediator	$-\frac{g_\chi}{2} \chi^\mu \gamma^\nu Z'_\mu \gamma^\lambda \chi - g_\nu \overline{N}_L \gamma^\mu Z'_\mu \nu_L$	$\frac{g_\chi^2 g_\nu^2}{12\pi} \frac{m_{\text{DM}}^2}{(4m_{\text{DM}}^2 - m_{Z'}^2)^2} v_{\text{CM}}^2$	$\frac{3g_\nu^2 g_\nu^2 m_{\text{DM}}^2 y^2}{32\pi m_{Z'}^2}$
Vector DM Vector Mediator	$-g_\chi \frac{1}{2} \chi^\mu \partial_\nu \chi^\nu Z'_\mu + \text{h.c.} - g_\nu \overline{N}_L \gamma^\mu Z'_\mu \nu_L$	$\frac{g_\chi^2 g_\nu^2}{\pi} \frac{m_{\text{DM}}^2}{(4m_{\text{DM}}^2 - m_{Z'}^2)^2} v_{\text{CM}}^2$	$\frac{g_\nu^2 g_\nu^2 m_{\text{DM}}^2 y^2}{8\pi m_{Z'}^2}$

TABLE I: This table presents the relevant terms in the Lagrangian, the approximate expressions for the annihilation cross section and the low-energy limit of the elastic scattering for all possible scenarios that involve DM- ν interactions (12 in total). Only the leading terms in v_{CM} and $y = (\epsilon - m_{\text{DM}}^2)/m_{\text{DM}}^2 \simeq 2E_\nu/m_{\text{DM}}$ (with ϵ the usual Mandelstam variable) are presented for the thermally averaged annihilation cross section and the elastic scattering cross section, respectively. We refer the reader to Appendix B for the full expressions of the elastic scattering cross sections.

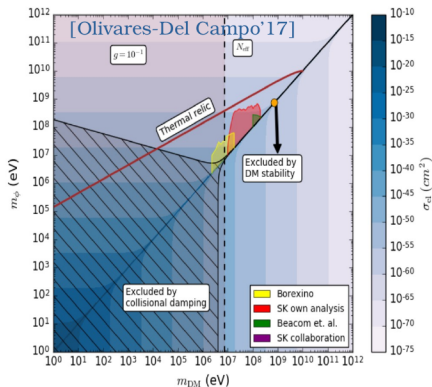
Particle physics models for DM- ν interactions

[Olivares-Del Campo'17]

Fermion DM coupled to a scalar mediator $-g\overline{\chi}_R\nu_L\phi + \text{h.c.}$

if the scalar mediator and the fermion DM candidate are degenerated

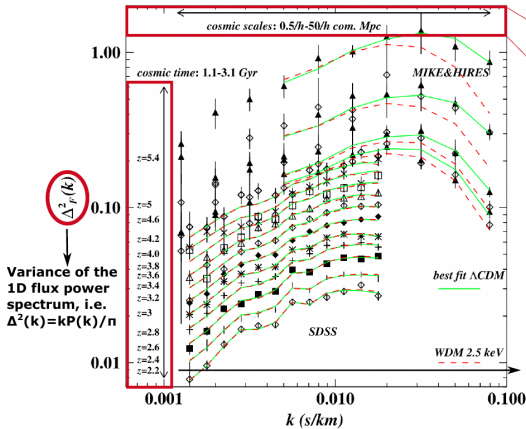
$\sigma_{\text{el}} = \frac{g^4}{32\pi m_{\text{DM}}^2}$ for Dirac DM and $\sigma_{\text{el}} = \frac{g^4}{16\pi m_{\text{DM}}^2}$ for Majorana DM



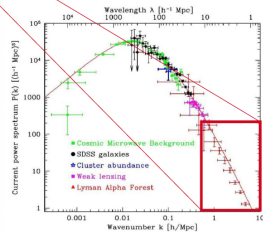
Lyman- α forest

Absorption lines produced by the inhomogeneous IGM along different line of sights to distant quasars: a fraction of photons is absorbed at the Lyman- α wave-length (corresponding to $\lambda_\alpha \sim 121$ nm), resulting in a depletion of the observed spectrum at a given frequency ($\lambda_{abs} < \lambda_\alpha$).

- Allows us to trace neutral hydrogen clouds, i.e. smallest structures
- Provides a tracer of the matter power spectrum at high redshifts ($2 < z < 6$) and small scales ($0.5 h/\text{Mpc} < k < 20 h/\text{Mpc}$).
- IGM modelling requires nonlinear evolution: this needs N-body hydrodynamical simulations. Computational expensive and only available for few benchmark models.

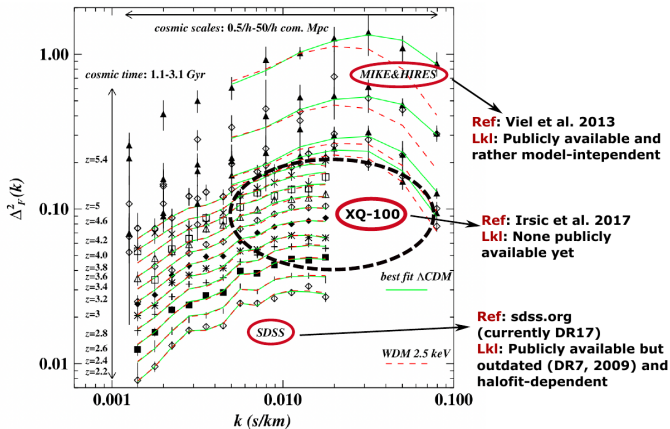


Adapted from Tegmark et al. 2004



- The higher the z of the source,
- 1) the more absorption one gets,
 - 2) the lower the mean transmission is,
 - 3) the more the density fluctuations amplify,
 - 4) the larger the amplitude of the spectrum

Adapted from Viel et al. 2013 4/25



Adapted from Viel et al. 2013

5/25

Matteo Lucca

Area criterium [Schneider 2016, Murgia, Merle, Viel, Totzauer, Schneider 2017]

- Consider ratio of 1D power spectra, computed with CLASS

$$r(k) = \frac{P_{1D}^X(k)}{P_{1D}^{\text{CDM}}(k)} \quad \text{with} \quad P_{1D}^X(k) = \int_k^\infty dk' k' P_X(k'),$$

- Compute area under the curve

$$A_X = \int_{k_{\min}}^{k_{\max}} dk' r(k')$$

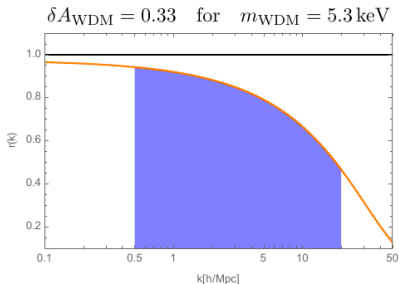
and

$$\delta A_X = \frac{A_{\text{CDM}} - A_X}{A_{\text{CDM}}}$$

- For freeze-in ($\delta = 1$):

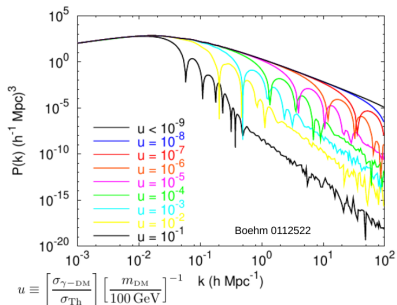
$$m_{\text{FI}} > 15.3 \text{ keV}$$

- Suitable for mixed scenario

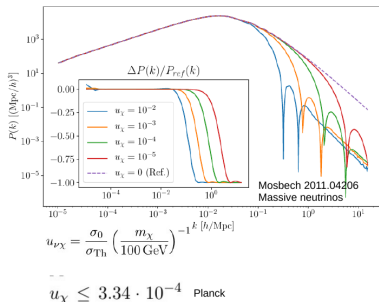


[see also D'Eramo, Lenoci, 2020; Egana-Ugrinovic, Essig, Gift, LoVerde 2021]

IDM $P(k)$



Planck $\sigma_{\text{DM-photon}} < 8 \times 10^{-31} \text{ (m}_{\text{DM}}/\text{GeV}) \text{ cm}^2$



NCDM from PBH evaporation

Cosmology

$$\frac{df_{\chi}(t, p)}{dt}$$

=

$$\mathcal{C}[f_{\chi}]$$

Particle Physics

Feeble/No
coupling to SM

$$\Gamma_{\chi \leftrightarrow \text{SM}} < H$$

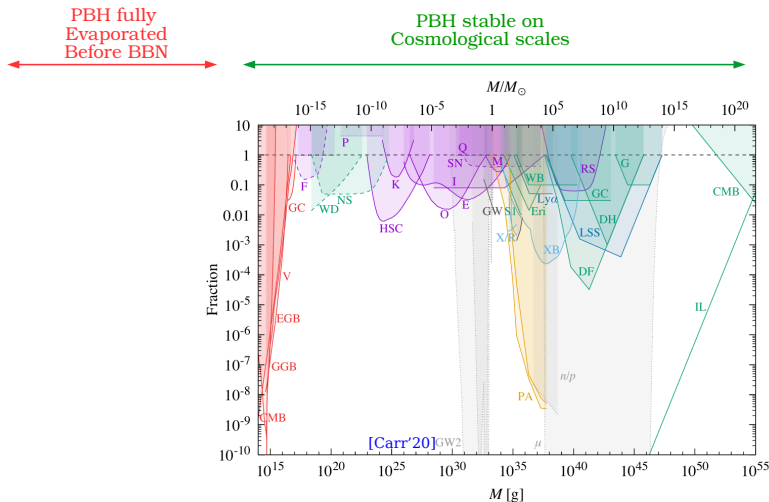
“Non-Thermal” DM
 $f_{\chi}(t, p) \neq f_{\chi}(t, p)^{f^{D, BE}}$

Produced through
gravitational
interactions
and freestream
while struct. forms

DM from
Primordial Black
Holes (PBH)
evaporat°

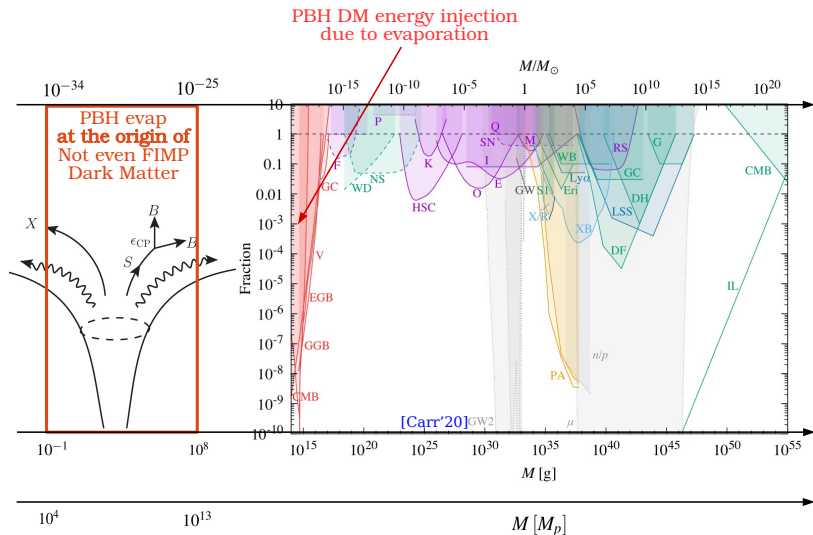
PBH and Dark Matter

see also e.g. [Bauman'07,Fujita'14,Allahverdi'17, Lennon'17,Morrison'17, Hooper'19+, Masina'20,Keith'20, Gondolo'20,Bernal'20+]



PBH and Dark Matter

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NCDM from PBH evaporation

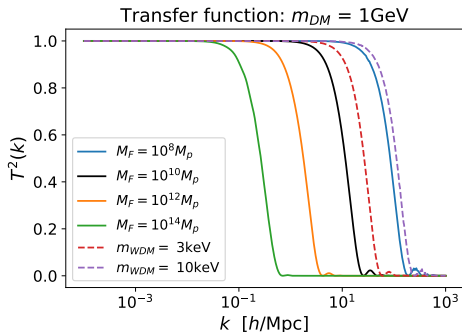
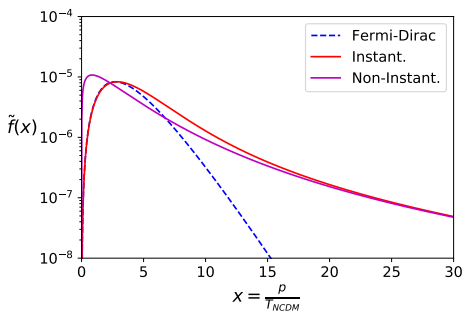
PBHs may be light enough to decay via **Hawking radiation** at an early enough epoch to avoid all previous constraints.

- DM particles (and SM) will be produced from PBH evaporation given **gravitational interactions** (not even FIMPs needed).
- For $m_{DM} < T_{BH}^{init} = M_p^2 / (8\pi M_{BH}^{init})$, behave as non-thermal NCDM.

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- For $m_{DM} < T_{BH}^{init} = M_p^2 / (8\pi M_{BH}^{init})$, behave as **non-thermal NCDM**.



$$\Rightarrow m_{DM}^{PBH} \geq 2 \text{ GeV} \times \left(M_F / (10^{10} M_p) \right)^{1/2} \quad [\text{for } m^{Ly-\alpha} > 3 \text{ keV and } \beta > \beta_c]$$

PBH evaporating after inflation and before BBN

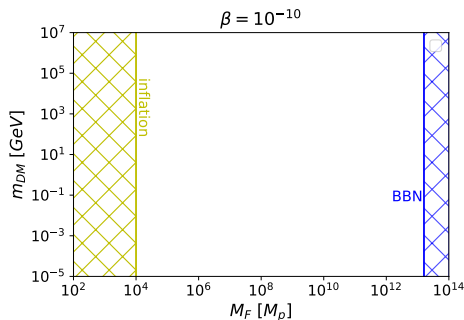
PBH generation: during **radiation domination** (after inflation) an initially large density perturbation at sufficiently small scale can collapse to form a PBH with mass of order the horizon mass. [Zeldovich & Novikov; Hawking; Carr & Hawking]

$$M_{BH}^{init} \equiv M_F = M_{horiz} = \gamma \rho_{tot} \times 4\pi / (3H_F^3)$$

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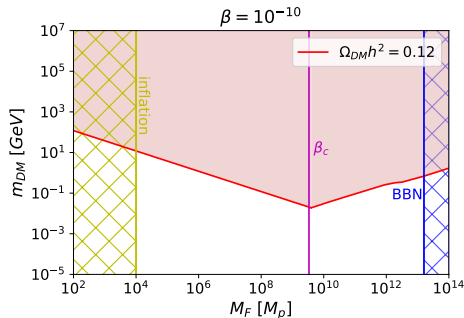


- PBH formed **after inflation**:
 $t_F > t_{infl} \rightarrow M_F > 10^4 M_p$
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 $t_{ev} < t_{BBN} \rightarrow M_F < 2 \times 10^{13} M_p$

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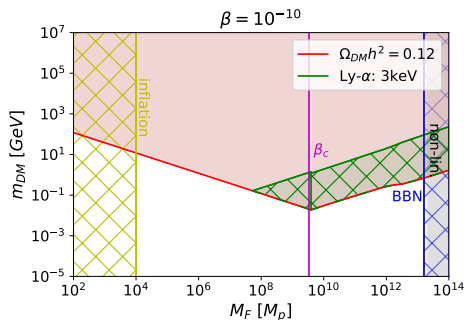


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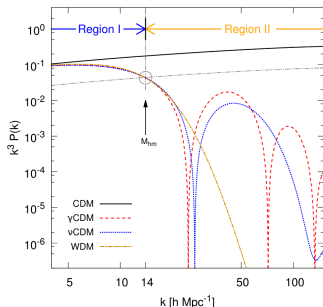
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Lyman- α bound: NCDM account for all the DM if $\beta \lesssim 5 \times 10^{-7}$ and $m_{DM} \gtrsim 2 \text{ MeV}$.

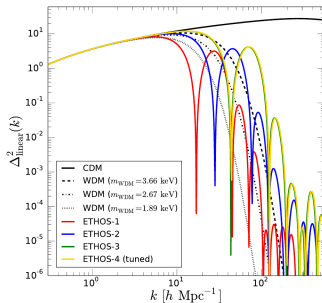
(S)IDM collisional Damping: linear regime

For dark matter interacting with (dark) relativistic degrees of freedom:

see also Zavala, Cyr-Racine, etc talks



[Schewtschenko'14]



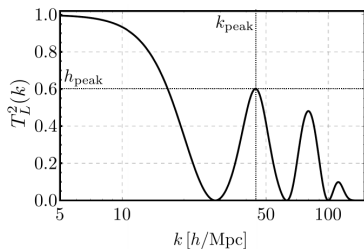
[VogelsBerger'15]

Towards generalized fit to non-CDM (SIDM included)? [Murgia'17]

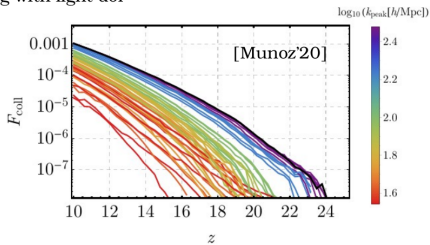
$$T(k) = (1 + (\alpha k)^\beta)^\gamma \rightarrow \text{might be usefull enough to derive Ly}\alpha \text{ forest and MW satellite count constraints}$$

IDMs with ETHOS parametrisation

ETHOS parametrization of DM interacting with light dof

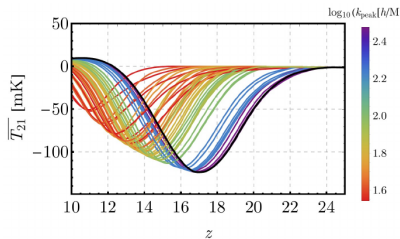


$h_{\text{peak}} \rightarrow 0$ corresponds to WDM

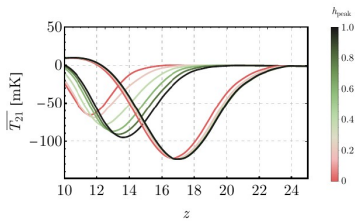


$k_{\text{peak}} \rightarrow$ large values corresponds to CDM

IDMs with ETHOS parametrisation

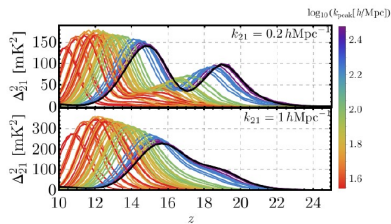


Cut at lower k_{peak} delay
structure formation more

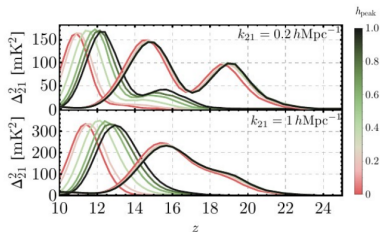


Higher values of h_{peak} gives more
power at small scales and delay
less structure formation

IDMs with ETHOS parametrisation



Cut at lower k_{peak} delay
structure formation more



Higher values of h_{peak} gives more
power at small scales and delay
less structure formation

HMF details

$$f(\sigma) = A \sqrt{\frac{2q}{\pi}} \left(1 + \left(\frac{\sigma^2}{q \delta_c^2} \right)^p \right) \left(\frac{\delta_c}{\sigma} \right) e^{-\frac{q \delta_c^2}{2\sigma^2}} \quad \text{Sheth and Tormen (ST)}$$

$$\sigma^2(M(R), z) = \left(\frac{D(z)}{D(0)} \right)^2 \int \frac{d^3k}{(2\pi)^3} P(k) |W(kR)|^2$$

spherical top-hat (TH) function in real space, $W_{\text{TH}}(kR) = \frac{3}{kR} (\sin(kR) - 3 \cos(kR)) \quad R^3 = 3M/(4\pi\rho_{m,0})$

sharp- k window

$$W_{\text{SK}}(kR) = \Theta(1 - kR)$$

$$M_{\text{SK}} = \frac{4\pi}{3} \rho_m (cR_{\text{SK}})^3.$$

smooth- k filter

$$W(k|R) = \frac{1}{1 + (kR)^\beta}$$

Top hat versus sharp k cutoff scale for γ CDM

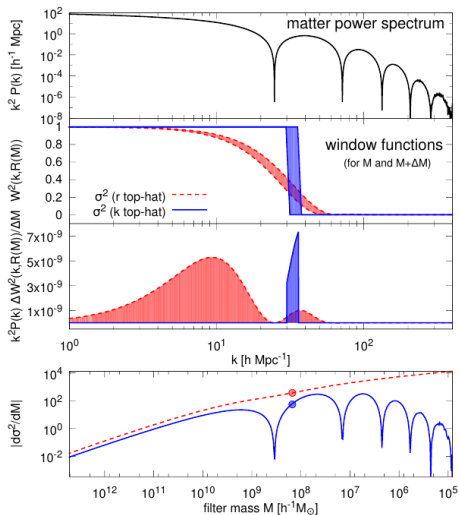


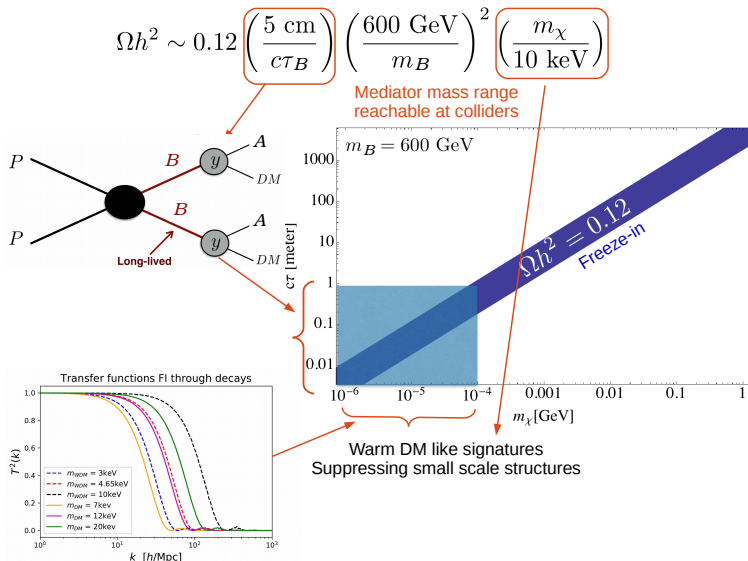
Figure 4. Real-space and k -space top-hat functions in Press-Schechter HMF predictions for γ CDM. The upper panel shows the matter power spectrum, while the second panel shows the Fourier transform of the two window functions (r top-hat and k top-hat). Each window function is evaluated for two filter masses, M and $M + \Delta M$. The difference between the two filter masses is highlighted by the shaded region in each case. The third panel shows the result of applying this differential filter to the matter distribution. Finally, the lower panel shows the integrated result for both window functions. The red and blue points are the results for the specific filter mass M used in the middle two panels.

\rightsquigarrow with r -top hat filter (TH) a large number of un-suppressed small k scales contribute to $\sigma(M)$

\rightsquigarrow not good to describe $\sigma(M)$ for suppressed $P(k)$ including WDM

FIMPs: LLPs and NCDM

e.g. [Hall'09, Co'15, Hessler'16, d'Eramo'17, Heeck'17, Boulebane'17, Brooijmans'18, Garny'18, Calibbi'18, No'19, Belanger 18, etc]



This is really the end